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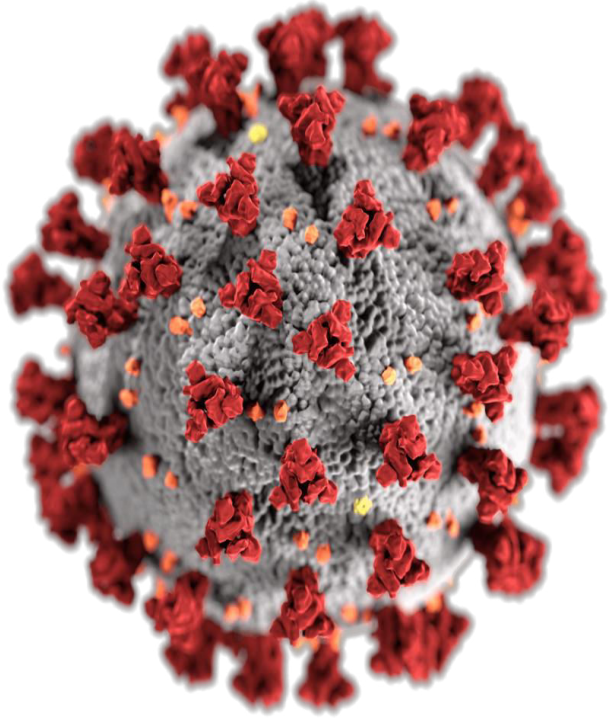
# Welcome to my Class

## Physics Ph 1109

11:45 AM

November 12, 2020

# COVID-19 Precautions



- Don't be afraid
- Be aware of the pandemic
- Use appropriate outfits if you compelled to go out
- Try to maintain proper diet
- Do not forget to exercise (at least one hour) regularly

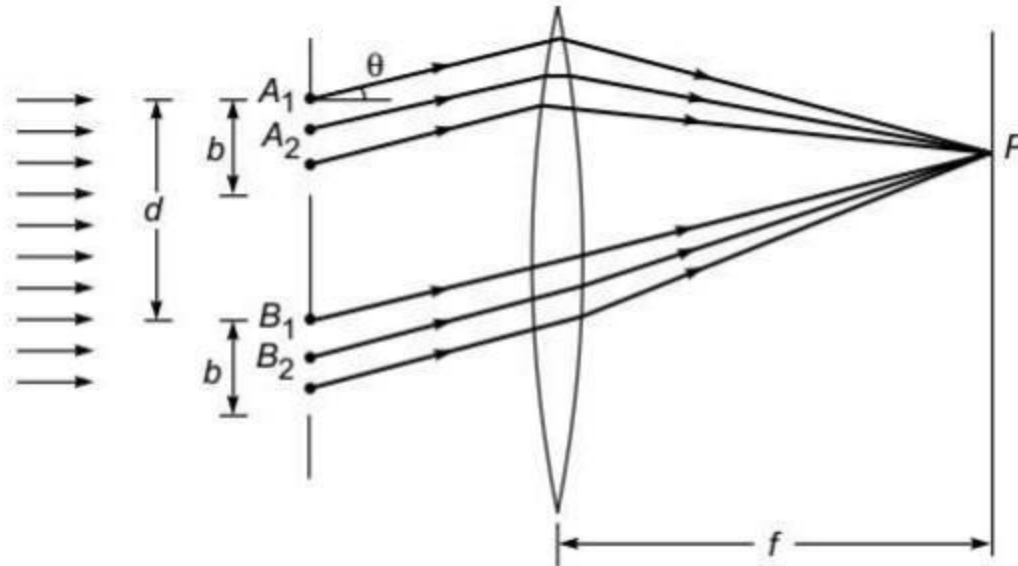
➤ Try to follow the guidelines of WHO and Bangladesh Government

➤ Try to stay at home

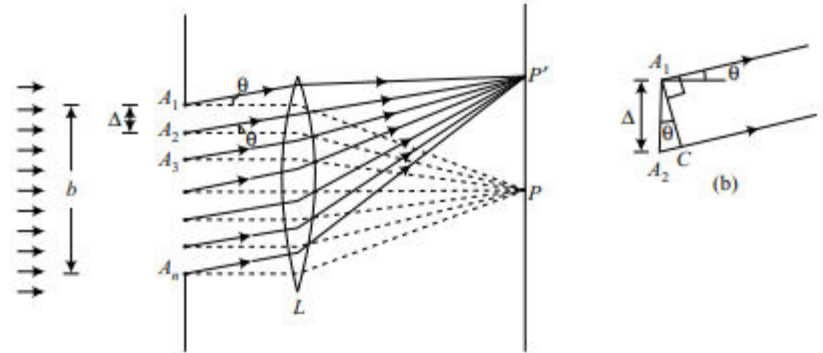
# Two-Slit Fraunhofer Diffraction Pattern

$$E_1 = A \frac{\sin \beta}{\beta} \cos (\omega t - \beta) \quad (1)$$

$$E_2 = A \frac{\sin \beta}{\beta} \cos (\omega t - \beta - \varphi_1) \quad (2)$$



where  $\varphi_1 = \frac{2\pi}{\lambda} d \sin\theta$



$$E = E_1 + E_2$$

$$= A \frac{\sin\beta}{\beta} [\cos(\omega t - \beta) + \cos(\omega t - \beta - \varphi_1)] \quad (3)$$

$$E = 2A \frac{\sin\beta}{\beta} \cos\gamma \cos\left(\omega t - \beta - \frac{1}{2}\varphi_1\right) \quad (4)$$

where  $\gamma = \frac{\varphi_1}{2} = \frac{\pi}{\lambda} d \sin\theta$  (5)

The intensity distribution will be of the form

$$I = 4I_0 \frac{\sin^2 \beta}{\beta^2} \cos^2 \gamma \quad (6)$$

## Positions of Maxima and Minima

The intensity is zero wherever

$$\beta = \pi, 2\pi, 3\pi, \dots \quad (7)$$

$$\text{or when } \gamma = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \dots \quad (8)$$

The corresponding angles of diffraction will be given by the following equations

$$b \sin \theta = m \lambda; \quad (m = 1, 2, 3, \dots) \quad (9)$$

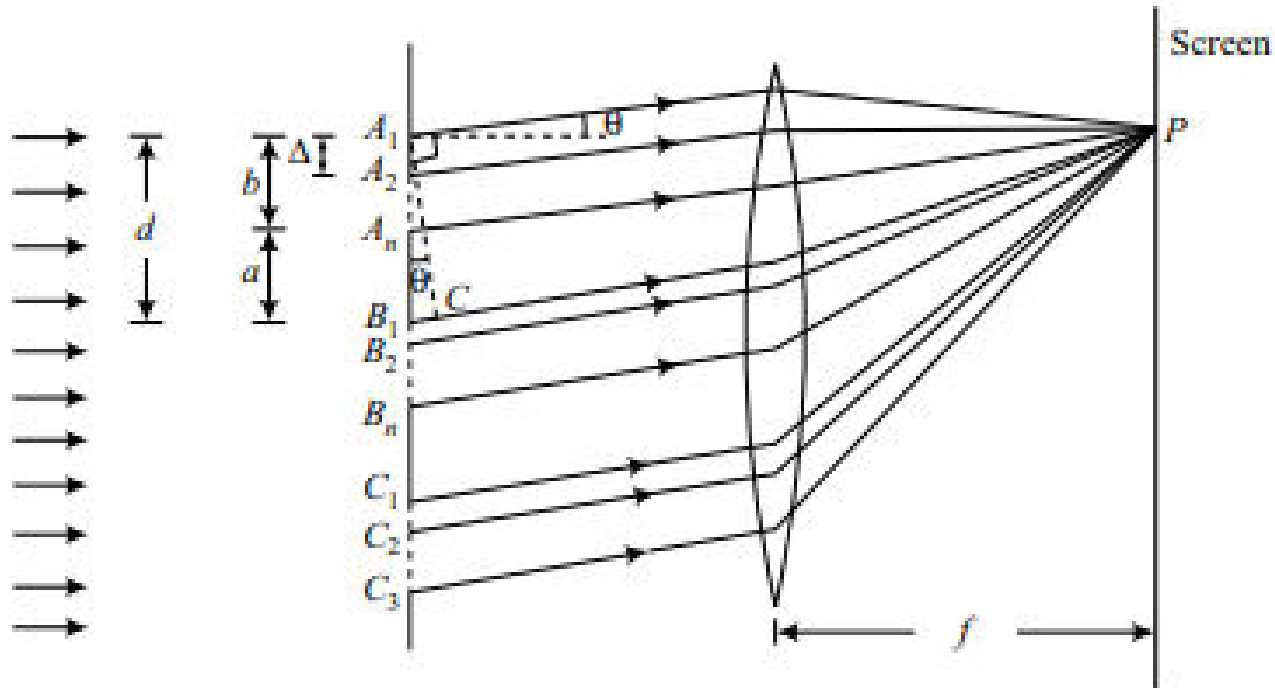
$$\text{and } d \sin \theta = \left(n + \frac{1}{2}\right) \lambda; \quad (n = 0, 1, 2, 3, \dots) \quad (10)$$

The interference maxima occur when

$$\gamma = 0, \pi, 2\pi, 3\pi, \dots \quad (11)$$

$$\text{or } d \sin \theta = 0, \lambda, 2\lambda, 3\lambda \dots \quad (12)$$

# N-Slit Fraunhofer Diffraction Pattern



$$\begin{aligned}
 E = A \frac{\sin\beta}{\beta} \cos(\omega t - \beta) + A \frac{\sin\beta}{\beta} \cos(\omega t - \beta - \varphi_1) + \dots \\
 + A \frac{\sin\beta}{\beta} \cos(\omega t - \beta - (N - 1)\varphi_1)
 \end{aligned} \tag{13}$$

$$\begin{aligned}
 E = A \frac{\sin\beta}{\beta} [\cos(\omega t - \beta) + \cos(\omega t - \beta - \varphi_1) + \dots \\
 + \cos(\omega t - \beta - (N - 1)\varphi_1)] \\
 = A \frac{\sin\beta}{\beta} \frac{\sin N\gamma}{\sin\gamma} \cos\left(\omega t - \beta - \frac{1}{2}(N - 1)\varphi_1\right)
 \end{aligned} \tag{14}$$

$$\text{where } \gamma = \frac{\varphi_1}{2} = \frac{\pi}{\lambda} d \sin\theta \tag{15}$$



The corresponding intensity distribution will be

$$I = I_0 \frac{\sin^2 \beta}{\beta^2} \frac{\sin^2 N\gamma}{\sin^2 \gamma} \quad (16)$$

## Positions of Maxima and Minima

When the value of  $N$  is very large, one obtains intense maxima at  $\gamma \approx m\pi$

$$d \sin \theta = m\lambda \quad (m = 0, 1, 2, 3, \dots) \quad (17)$$

The intensity is zero when

$$b \sin \theta = n \lambda \quad (n = 1, 2, 3, \dots) \quad (18)$$

$$\text{or } N \gamma = p \pi, \quad p \neq N, 2N, \dots \quad (19)$$

$$d \sin \theta = \frac{\lambda}{N}, \frac{2\lambda}{N}, \dots, \frac{(N-1)\lambda}{N}, \frac{(N+2)\lambda}{N}, \dots, \frac{(2N-1)\lambda}{N}, \frac{(2N+1)\lambda}{N}, \frac{(2N+2)\lambda}{N}, \dots \quad (20)$$

## Missing Orders

$$d \sin \theta = m \lambda \quad (m = 0, 1, 2, 3, \dots) \quad (21)$$

$$b \sin \theta = n \lambda \quad (n = 1, 2, 3, \dots) \quad (22)$$

## Width of the Principal Maxima

$$d \sin \theta_m = m \lambda \quad (m = 0, 1, 2, 3, \dots) \quad (23)$$

If  $\theta_m + \Delta\theta_{1m}$  and  $\theta_m - \Delta\theta_{2m}$  represent the angles of diffraction corresponding to the first minimum on either side of the principal maximum, then  $(\Delta\theta_{1m} + \Delta\theta_{2m})/2$  is known as the angular half width of the  $m$ th order principal maximum. For a large value of  $N$ ,  $\Delta\theta_{1m} \approx \Delta\theta_{2m}$  which we write as  $\Delta\theta_m$ . Clearly,

$$d \sin(\theta_m \pm \Delta\theta_m) = m\lambda \pm \frac{\lambda}{N} \quad (24)$$

*But*

$$\begin{aligned} \sin(\theta_m \pm \Delta\theta_m) &= \sin\theta_m \cos\Delta\theta_m \pm \cos\theta_m \sin\Delta\theta_m \\ &\cong \sin\theta_m \pm \Delta\theta_m \cos\theta_m \end{aligned} \quad (25)$$

$$\therefore \Delta\theta_m \cong \frac{\lambda}{Nd\cos\theta_m} \quad (26)$$

## The Diffraction Grating

The diffraction grating, a useful device for analyzing light sources, consists of a large number of equally spaced parallel slits. A transmission grating can be made by cutting parallel lines on a glass plate with a precision ruling machine

15000 lines/inch

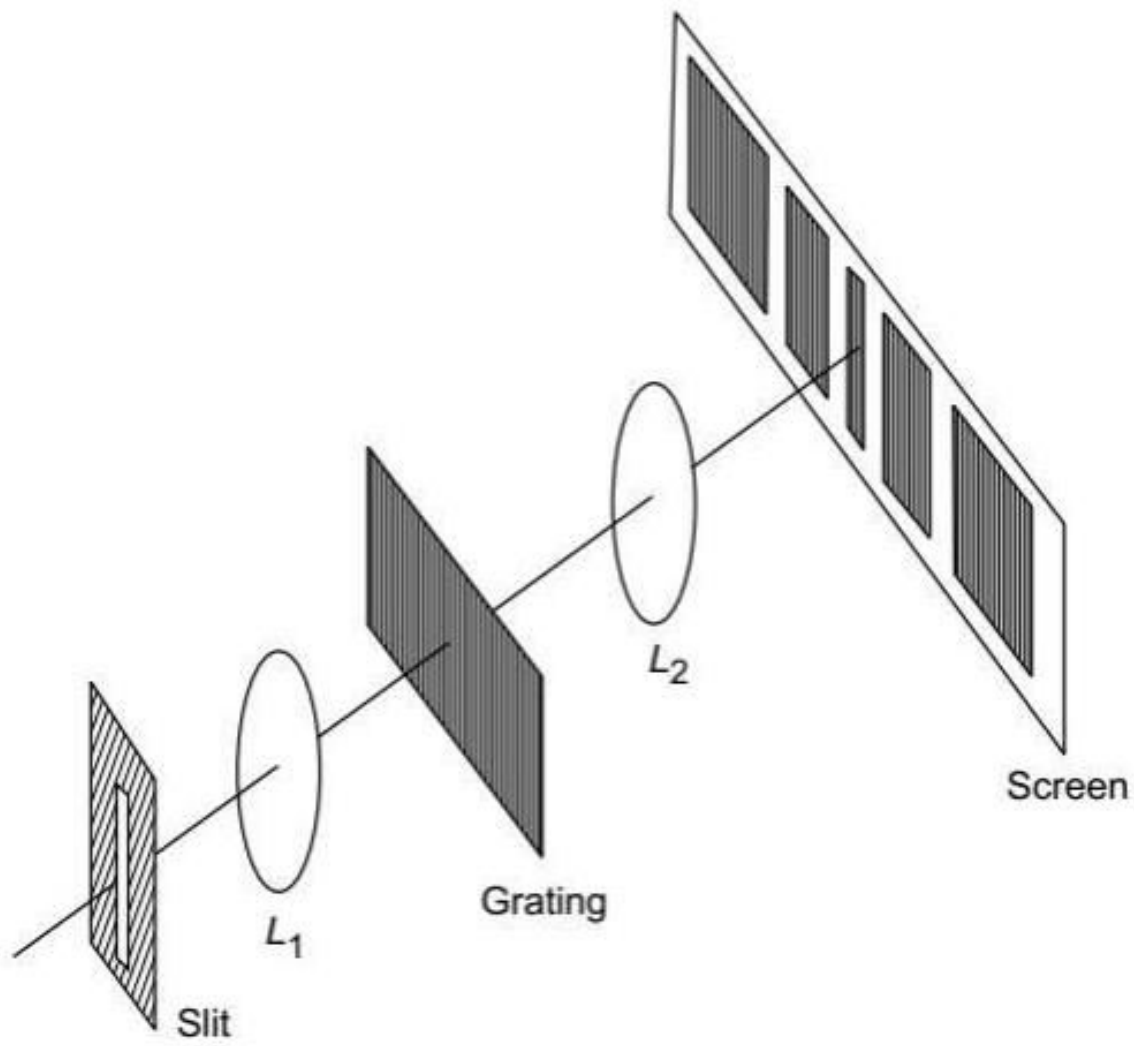
Rowland (1882) – 14438 lines/inch

# The Grating Spectrum

$$d \sin \theta_m = m \lambda \quad (m = 0, 1, 2, 3, \dots) \quad (27)$$

If we differentiate eqn. (27), we obtain

$$\frac{\Delta \theta}{\Delta \lambda} = \frac{m}{d \cos \theta} \quad (28)$$

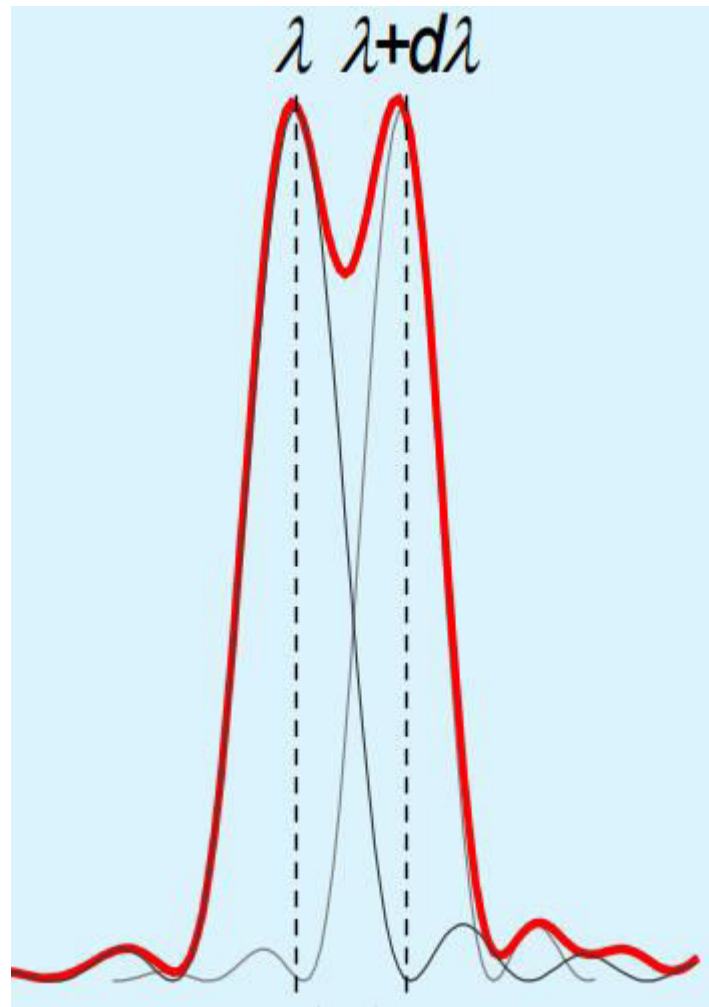


# Resolving Power of a Grating

*Resolving Power,*  $R = \frac{\lambda}{\Delta\lambda}$  (29)

**Rayleigh criterion:** Two wavelengths in a line spectrum are resolved if the maximum in the diffraction pattern from light with one wavelength coincides with the minimum in the diffraction pattern from light with the other wavelength.





$$d \sin \theta = m(\lambda + \Delta \lambda) \quad (30)$$

$$d \sin \theta = m\lambda + \frac{\lambda}{N} \quad (31)$$

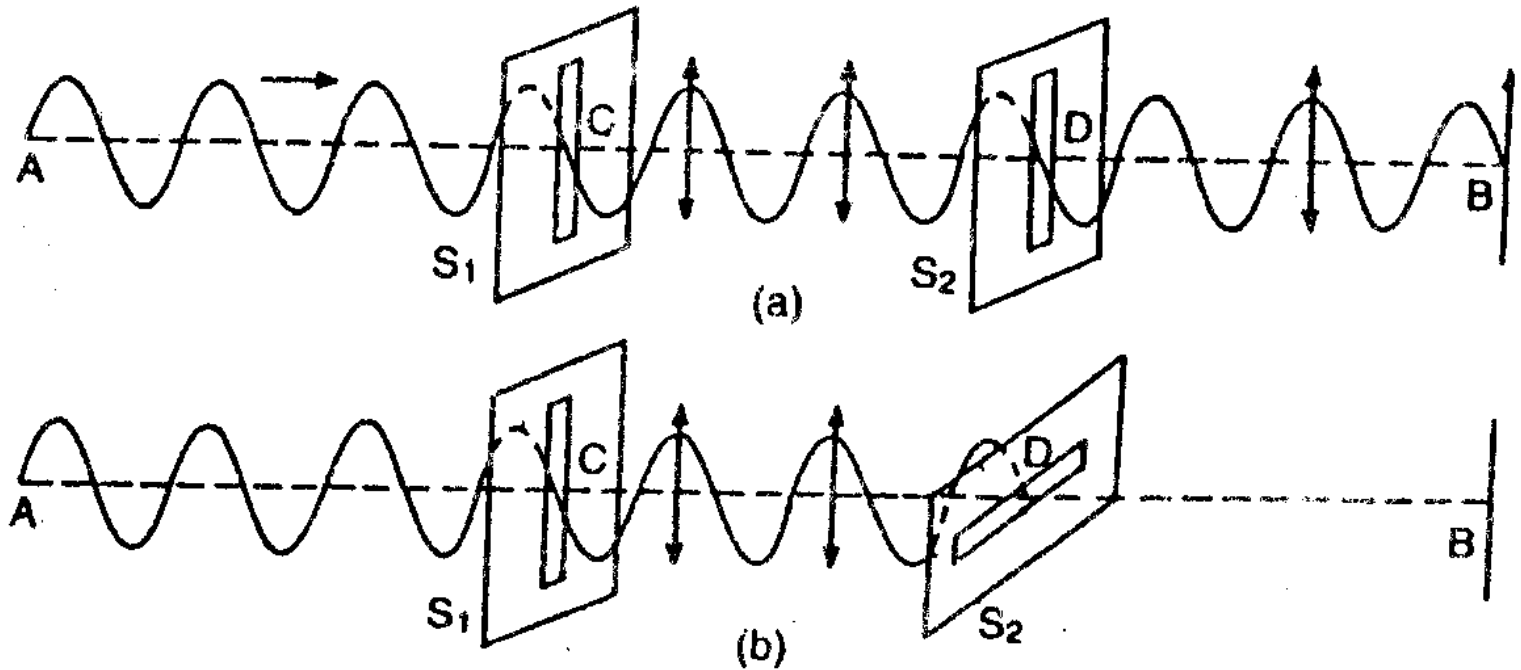
$$\text{Thus} \quad R = \frac{\lambda}{\Delta \lambda} = mN \quad (32)$$

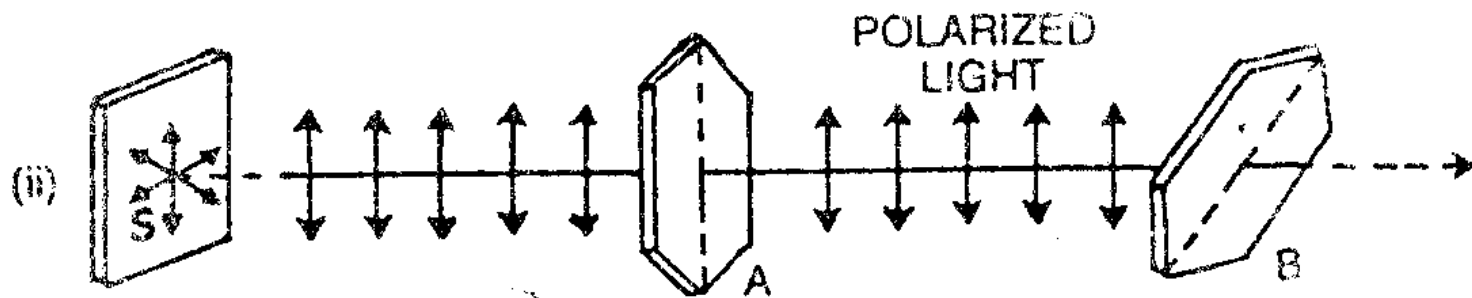
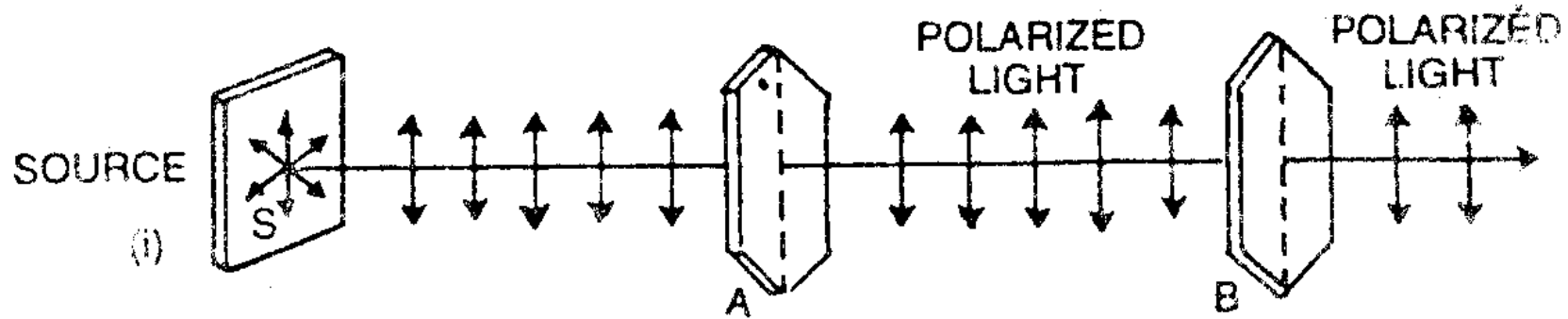
**Interference and Diffraction**

# Polarization of Light

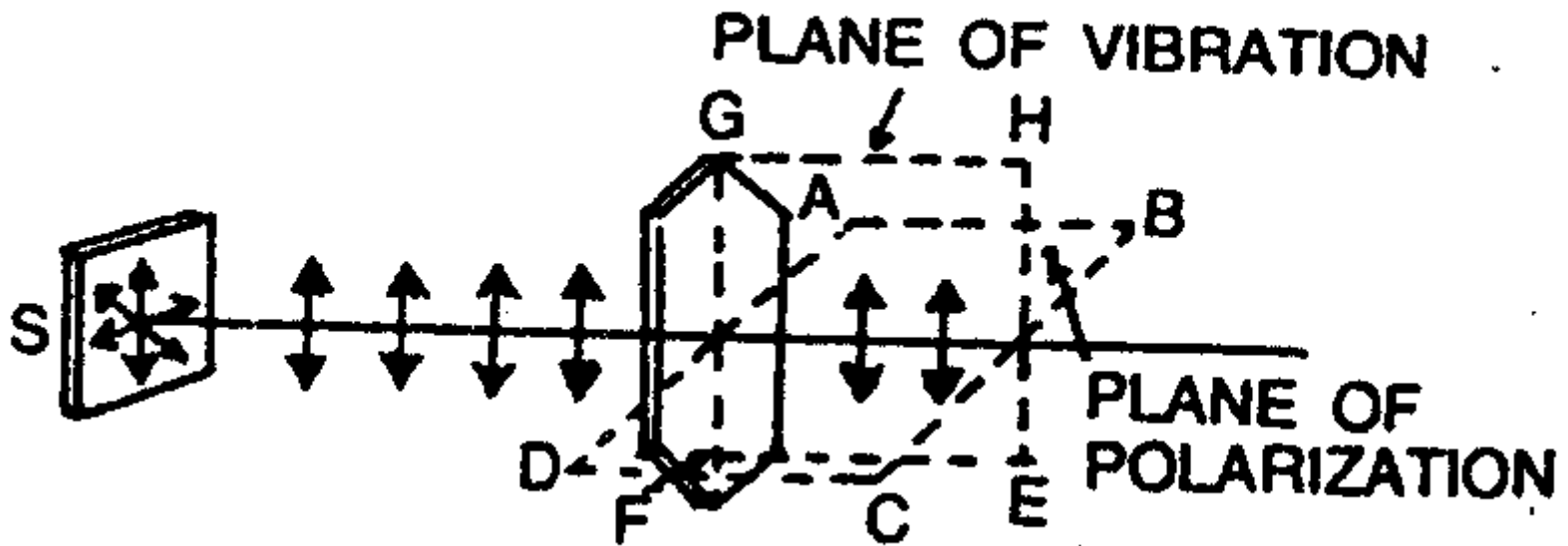
Experiments on interference and diffraction have shown that light is a form of wave motion. These effects do not tell us about the type of motion i.e., whether the light waves are longitudinal or transverse, or whether the vibrations are linear, circular or torsional. The phenomenon of polarization has helped to establish beyond doubt that light waves are transverse waves.

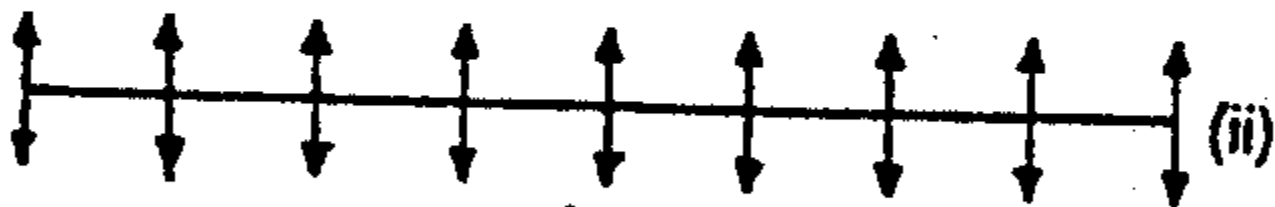
# Polarization of Transverse Waves





# Plane of Polarization





I Thank you

